# Package 'tvmediation'

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Title Time Varying Mediation Analysis

**Description** Provides functions for estimating mediation effects that vary over time as described in Cai X, Coffman DL, Piper ME, Li R. Estimation and inference for the mediation effect in a time-varying mediation model. BMC Med Res Methodol. 2022;22(1):1-12.

RoxygenNote 7.1.2

**Depends** R (>= 4.0.0)

Imports stats (>= 4.0.2), dplyr (>= 1.0.2), ggplot2 (>= 3.3.2), locpol (>= 0.7-0)

Suggests knitr, rmarkdown

License GPL-3

URL https://github.com/dcoffman/tvmediation/wiki

BugReports https://github.com/dcoffman/tvmediation/issues

LazyData true

VignetteBuilder knitr

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<pre>bootci_coeff_2trt</pre>	Bootstrap function for computing CIs for coefficients for a continuous
	outcome and two treatment groups

# Description

Part of the set of internal functions for estimating bootstrapped CIs for the coefficients of the mediation model for continuous outcome and two treatment groups.

# Usage

bootci\_coeff\_2trt(trt, t.seq, M, Y, t.est, deltat, replicates)

trt	a vector indicating treatment group
t.seq	a vector of time points for each observation
М	matrix of mediator values in wide format
Υ	matrix of outcome values in wide format
t.est	time points at which to make the estimation. Default = t.seq
deltat	a small constant which controls the time-lag of the effect of the mediator on the outcome.
replicates	number of replicates for bootstrapping confidence intervals. Default = 1000

CI.upper.alpha	CI upper limit for coefficient hat.alpha
CI.lower.alpha	CI lower limit for coefficient hat.alpha
CI.upper.gamma	CI upper limit for coefficient hat.gamma
CI.lower.gamma	CI lower limit for coefficient hat.gamma
CI.upper.beta	CI upper limit for coefficient hat.beta
CI.lower.beta	CI lower limit for coefficient hat.beta
CI.upper.tau	CI upper limit for coefficient hat.tau
CI.lower.tau	CI lower limit for coefficient hat.tau

bootci\_coeff\_3trt Bootstrap samples to estimate confidence intervals for coefficients for a continuous outcome and three treatment groups.

# Description

Part of the set of internal functions for estimating bootstrapped confidence intervals for the coefficients of the mediation model for a continuous outcome and three treatment groups.

#### Usage

```
bootci_coeff_3trt(
  T1,
  T2,
  t.seq,
  mediator,
  outcome,
  t.est,
  original.coeff,
  boot.sample = 1000
)
```

T1	a vector indicating assignment to treatment 1
Т2	a vector indicating assignment to treatment 2
t.seq	a vector of time points for each observation
mediator	matrix of mediator values in wide format
outcome	matrix of outcome values in wide format
t.est	time points at which to make the estimation. Default = t.seq
original.coeff	a list of the estimated coefficients.
boot.sample	number of replicates for bootstrapping confidence intervals. Default = 1000.

alw1	CI lower limit for estimated Treatment 1 effect on mediator
aup1	CI upper limit for estimated Treatment 1 effect on mediator
alw2	CI lower limit for estimated Treatment 2 effect on mediator
aup2	CI upper limit for estimated Treatment 2 effect on mediator
glw1	CI lower limit for estimated Treatment 1 direct effect on outcome
gup1	CI upper limit for estimated Treatment 1 direct effect on outcome
glw2	CI lower limit for estimated Treatment 2 direct effect on outcome
gup2	CI upper limit for estimated Treatment 2 direct effect on outcome
tlw1	CI lower limit for estimated Treatment 1 total effect on outcome
tup1	CI upper limit for estimated Treatment 1 total effect on outcome
tlw2	CI lower limit for estimated Treatment 2 total effect on outcome
tup2	CI upper limit for estimated Treatment 2 total effect on outcome
blw	CI lower limit for estimated effect of mediator on outcome
bup	CI upper limit for estimated effect of mediator on outcome

bootci\_coeff\_binary Bootstrap samples to estimate confidence intervals for binary outcome coefficients.

#### Description

Internal function for estimating bootstrapped confidence intervals for the coefficients of the mediation model for a binary outcome.

#### Usage

```
bootci_coeff_binary(
   treatment,
   t.seq,
   m,
   outcome,
   span = 0.75,
   replicates = 1000
)
```

treatment	a vector indicating treatment group
t.seq	a vector of unique time points for each observation
m	matrix of mediator values in wide format
outcome	matrix of outcome values in wide format
span	Numeric value of the span to be used for LOESS regression. Default = $0.75$ .
replicates	Number of replicates for bootstrapping confidence intervals. Default = 1000.

#### bootci\_tvmb

# Value

t.seq	time points of estimation
CI.lower.a	CI lower limit for alpha_hat
CI.upper.a	CI upper limit for alpha_hat
CI.lower.g	CI lower limit for gamma_hat
CI.upper.g	CI upper limit for gamma_hat
CI.lower.b	CI lower limit for beta_hat
CI.upper.b	CI upper limit for beta_hat
CI.lower.t	CI lower limit for tau_hat
CI.upper.t	CI upper limit for tau_hat

bootci\_tvmb

Bootstrap samples to estimate confidence intervals for the mediation effect for a binary outcome.

# Description

Part of the set of internal functions for estimating bootstrapped confidence intervals for the mediation effect for a binary outcome when user argument CI="boot".

# Usage

```
bootci_tvmb(
  treatment,
  t.seq,
  m,
  outcome,
  coeff_data,
  span = 0.75,
  replicates = 1000
)
```

treatment	a vector indicating treatment group
t.seq	a vector of unique time points for each observation
m	matrix of mediator values in wide format
outcome	matrix of outcome values in wide format
coeff_data	a merged dataset of indirect and direct effects and CIs estimated from $bootci\_coeff\_binary$
span	Numeric value of the span to be used for LOESS regression. Default = $0.75$ .
replicates	number of replicates for bootstrapping CIs. Default = 1000.

timeseq	time points of estimation
alpha_hat	time-varying treatment effect on the mediator
CI.lower.a	CI lower limit for estimated coefficient alpha_hat
CI.upper.a	CI upper limit for estimated coefficient alpha_hat
gamma_hat	time-varying treatment effect on the outcome (direct effect)
CI.lower.g	CI lower limit for estimated coefficient gamma_hat
CI.upper.g	CI upper limit for estimated coefficient gamma_hat
beta_hat	time-varying effect of the mediator on the outcome
CI.lower.b	CI lower limit for estimated coefficient beta_hat
CI.upper.b	CI upper limit for estimated coefficient beta_hat
tau_hat	time-varying treatment effect on outcome (total effect)
CI.lower.t	CI lower limit for estimated coefficient tau_hat
CI.upper.t	CI upper limit for estimated coefficient tau_hat
medEffect	time varying mediation effect
CI.lower	CI lower limit for medEffect
CI.upper	CI upper limit for medEffect

bootci_	tvm_	_3trt
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Bootstrap samples to estimate confidence intervals for continuous outcome and three treatment groups.

# Description

Internal function for estimating bootstrapped confidence intervals for the mediation effect of continuous outcome and three treatment groups when user argument CI="boot".

# Usage

```
bootci_tvm_3trt(boot.sample, orig.data, t.est)
```

boot.sample	number of replicates for bootstrapping confidence intervals. Default = 1000.
orig.data	a list of original data T1, T2, mediator, outcome and t.seq.
t.est	time points at which to make the estimation. Default = t.seq.

#### coeff

# Value

plw1	CI lower limit for estimated mediation effect of T1	
pup1	CI upper limit for estimated mediation effect of T1	
plw2	CI lower limit for estimated mediation effect of T2	
pup2	CI upper limit for estimated mediation effect of T2	
orig.se1.all	estimated standard errors for the mediation effect of T1	
orig.se2.all	estimated standard errors for the mediation effect of T2	
orig.mediation1		
	time varying mediation effect for T1	
orig.mediation2		
	time varying mediation effect for T2	

coeff

Function to estimate coefficients at time t

# Description

Part of the set of internal functions called within the tvmcurve\_3trt function to assist in the estimation of time varying mediation effect.

# Usage

coeff(j, T1, T2, x, y)

# Arguments

j	a number indicating time point of observation
T1	a vector indicating assignment to treatment 1
T2	a vector indicating assignment to treatment 2
x	matrix of mediator values in wide format
У	matrix of outcome outcomes in wide format

# Value

coeff.est	estimated coefficients of the mediation model	
nomissing.index		
	index of complete coses	

index of complete cases

estBootCIs

#### Description

Part of the set of internal functions for estimating bootstrapped confidence intervals for continuous outcome and two treatment groups when user argument CI="boot".

#### Usage

estBootCIs(trt, t.seq, M, Y, t.est, deltat, replicates)

#### Arguments

trt	a vector indicating treatment group
t.seq	a vector of time points at each obs
М	matrix of mediator values
Υ	matrix of outcome values
t.est	time points at which to make the estimation
deltat	a small constant which controls the time-lag of the effect of the mediator on the outcome, half the time between two time points
replicates	number of replicates for bootstrapping confidence intervals.

#### Value

boot.sebootstrapped standard error for the estimated mediation effect

CI.upperpercentile bootstrapped CI upper limit for the estimated mediation effect

CI.lowerpercentile bootstrapped CI lower limit for the estimated mediation effect

estCoeff

Function to estimate coefficients at time t.

#### Description

Part of the set of internal functions called within the tvma function to assist in the estimation of the time varying mediation effect.

#### Usage

estCoeff(newMO.j.est)

#### LongToWide

#### Arguments

newMO.j.est a list containing mean centered mediators and outcomes

#### Value

coeff.est estimated coefficients of the mediation model	coeff.est	estimated	coefficients	of the	mediation	model
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LongToWide	Function to transpose the data from long to wide format
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#### Description

Transposing a dataset with repeated measurements/responses for each subject from longitudinal to wide format.

#### Usage

LongToWide(subject.id, time.sequence, outcome, verbose = FALSE)

#### Arguments

<pre>subject.id</pre>	a column of subject identifiers
time.sequence	a column of time points
outcome	a column to be transposed
verbose	TRUE or FALSE (default = FALSE) prints output to screen (OPTIONAL IN- PUT)

#### Details

If data is not sorted by subject.id, a warning message will appear. The function will then sort the data by subject.id. It is recommended that the user sorts the data prior to using this function.

#### Value

mat.wide a matrix in wide format, in which each column is the outcome for each subject and each row is the time sequence

# Examples

smoker

newMediatorOutcome

*Function to compute new Mediator and Outcome using time t and t-1 mean centered on the individual.* 

# Description

Part of the set of internal functions called within the tvma function to assist in the estimation of time varying mediation effect.

#### Usage

```
newMediatorOutcome(trt, M, Y)
```

#### Arguments

trt	numeric binary treatment group indicator for each individual
М	(t.seq x N) matrix where N = number of observations. Column 1 is mediator at time t-1. Column 2 is mediator at time t.
Υ	(Nx1) matrix were N = number of observations. Column 1 is outcome at time $t-1$ .

#### Value

newMO	list containing new mediators, outcomes, and index of complete cases

smoker	Wisconsin Smokers' Health Study 2
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#### Description

The dataset is simulated based on the Wisconsin Smokers' Health Study 2.

#### Usage

data(smoker)

#### Format

A data frame with 40,130 observations on 12 variables.

- 1. SubjectID: Subject ID
- 2. **treatment:** Treatment group (2 = patch, 3 = varenicline, 4 = combination nicotine replacement therapy)
- 3. **patch:** Received patch (0 = No, 1 = Yes)
- 4. **varenicline:** Received varenicline (0 = No, 1 = Yes)

#### smoothest

- 5. **comboNRT:** Received combination nicotine replacement therapy (0 = No, 1 = Yes)
- 6. DaysFromTQD: Number of days from quit date
- 7. **time.of.day:** Time of day (0 = am, 1 = pm)
- 8. timeseq: Number of days from quit date (.5 indicates pm)
- 9. WantToSmokeLst15min: How did you feel in the last 15 min: wanting to smoke (1 = not at all, 7 = extremely)
- 10. **NegMoodLst15min:** How did you feel in the last 15 min: Negative mood (1 = not at all, 7 = extremely)
- 11. **cessFatig:** Cessation fatigue I am tired of trying to quit smoking (1 = strongly disagree, 7 = strongly agree)
- 12. CigCount: Cigarettes smoked over entire day
- 13. **smoke\_status:** Did you smoke (0 = No, 1 = Yes)

#### See Also

tvmb, tvma\_3trt tvma, LongToWide

#### Examples

data(smoker)

smoothest	Function to compute local polynomial estimation using rule of thumb
	for bandwidth selection

#### Description

Part of the set of internal functions called within the tvma function to assist in the estimation of the time varying mediation effect.

#### Usage

```
smoothest(t.seq, t.coeff, t.est, deltat)
```

t.seq	a vector of time points at each observation
t.coeff	estimated coefficients
t.est	time points at which to make the estimation
deltat	a small constant which controls the time-lag of the effect of the mediator on the outcome, half the time between two time points

bw_alpha	a number computed via Fan and Gijbels' (1996) rule of thumb for bandwidth selector for alpha coefficient.
bw_gamma	a number computed via Fan and Gijbels' (1996) rule of thumb for bandwidth selector for gamma coefficient.
bw_beta	a number computed via Fan and Gijbels' (1996) rule of thumb for bandwidth selector for beta coefficient.
bw_beta	a number computed via Fan and Gijbels' (1996) rule of thumb for bandwidth selector for tau coefficient.
hat.alpha	estimated treatment effect on mediator
hat.gamma	estimated treatment effect on outcome, adjusted for mediator
hat.beta	estimated mediator effect on outcome
hat.tau	estimated treatment effect on outcome, not adjusting for mediator
est.M	estimated mediation effect, product of hat.alpha and hat.beta

tvma	Time Varying Mediation Function:	Continuous Outcome and Two
	Treatment Groups	

# Description

Function to estimate the time-varying mediation effect and bootstrap standard errors for two treatment groups and a continuous outcome.

# Usage

```
tvma(
  treatment,
  t.seq,
 mediator,
 outcome,
  t.est = t.seq,
 plot = FALSE,
 CI = "boot",
  replicates = 1000,
 verbose = FALSE
```

# )

treatment	a vector indicating treatment group
t.seq	a vector of time points for each observation
mediator	matrix of mediator values in wide format

outcome	matrix of outcome values in wide format
t.est	a vector of time points at which to estimate. Default = t.seq (OPTIONAL AR-GUMENT)
plot	TRUE or FALSE for producing plots. Default = "FALSE" (OPTIONAL AR-GUMENT)
CI	"none" or "boot" method of deriving confidence intervals. Default = "boot" (OPTIONAL ARGUMENT)
replicates	number of replicates for bootstrapping confidence intervals. Default = 1000 (OPTIONAL ARGUMENT)
verbose	TRUE or FALSE for printing results to screen. Default = "FALSE" (OPTIONAL ARGUMENT)

hat.alpha	estimated time-varying treatment effect on mediator
CI.lower.alpha	CI lower limit for estimated coefficient hat.alpha
CI.upper.alpha	CI upper limit for estimated coefficient hat.alpha
hat.gamma	estimated time-varying treatment effect on outcome (direct effect)
CI.lower.gamma	CI lower limit for estimated coefficient hat.gamma
CI.upper.gamma	CI upper limit for estimated coefficient hat.gamma
hat.beta	estimated time-varying effect of the mediator on outcome
CI.lower.beta	CI lower limit for estimated coefficient hat.beta
CI.upper.beta	CI upper limit for estimated coefficient hat.beta
hat.tau	estimated time-varying treatment effect on outcome (total effect)
CI.lower.tau	CI lower limit for estimated coefficient hat.tau
CI.upper.tau	CI upper limit for estimated coefficient hat.tau
est.M	time varying mediation effect
boot.se.m	estimated standard error for est.M
CI.lower	CI lower limit for est.M
CI.upper	CI upper limit for est.M

#### **Plot Returns**

- 1. Alpha\_CI plot for hat.alpha with CIs over t.est
- 2. Gamma\_CI plot for hat.gamma with CIs over t.est
- 3. Beta\_CI plot for hat.beta with CIs over t.est
- 4. Tau\_CI plot for hat.tau with CIs over t.est
- 5. MedEff plot for est.M over t.est
- 6. MedEff\_CI plot for est.M with CIs over t.est

#### Note

1. **\*\*** IMPORTANT **\*\*** An alternate way of formatting the data and calling the function is documented in detail in the tutorial for the tvmb() function.

#### References

- Fan, J. and Gijbels, I. Local polynomial modelling and its applications: Monographs on statistics and applied probability 66. CRC Press; 1996.
- Fan J, Zhang W. Statistical Estimation in Varying Coefficient Models. The Annals of Statistics. 1999;27(5):1491-1518.
- Fan J, Zhang JT. Two-step estimation of functional linear models with applications to longitudinal data. Journal of the Royal Statistical Society: Series B (Statistical Methodology). 2000;62(2):303-322.
- 4. Cai X, Coffman DL, Piper ME, Li R. Estimation and inference for the mediation effect in a time-varying mediation model. BMC Med Res Methodol. 2022;22(1):1-12.
- Baker TB, Piper ME, Stein JH, et al. Effects of Nicotine Patch vs Varenicline vs Combination Nicotine Replacement Therapy on Smoking Cessation at 26 Weeks: A Randomized Clinical Trial. JAMA. 2016;315(4):371.
- 6. B. Efron, R. Tibshirani. Bootstrap Methods for Standard Errors, Confidence Intervals, and Other Measures of Statistical Accuracy. Statistical Science. 1986;1(1):54-75.

#### Examples

```
## Not run: data(smoker)
# REDUCE DATA SET TO ONLY 2 TREATMENT CONDITIONS (EXCLUDING COMBINATION NRT)
smoker.sub <- smoker[smoker$treatment != 4, ]</pre>
# GENERATE WIDE FORMATTED MEDIATORS
mediator <- LongToWide(smoker.sub$SubjectID,</pre>
                        smoker.sub$timeseq,
                        smoker.sub$NegMoodLst15min)
# GENERATE WIDE FORMATTED OUTCOMES
outcome <- LongToWide(smoker.sub$SubjectID,</pre>
                       smoker.sub$timeseq,
                       smoker.sub$cessFatig)
# GENERATE A BINARY TREATMENT VARIABLE
trt <- as.numeric(unique(smoker.sub[,c("SubjectID","varenicline")])[,2])-1</pre>
# GENERATE A VECTOR OF UNIQUE TIME POINTS
t.seq <- sort(unique(smoker.sub$timeseq))</pre>
# COMPUTE TIME VARYING MEDIATION ANALYSIS USING BOOTSTRAPPED CONFIDENCE INTERVALS
results <- tvma(trt, t.seq, mediator, outcome)</pre>
# COMPUTE TIME VARYING MEDIATION ANALYSIS FOR SPECIFIED POINTS IN TIME USING 250 REPLICATES
results <- tvma(trt, t.seq, mediator, outcome,
```

tvma\_3trt

```
t.est = c(0.2, 0.4, 0.6, 0.8),
    replicates = 250)
## End(Not run)
```

tvma\_3trt

*Time Varying Mediation Function: Continuous Outcome and Three Treatment Groups* 

#### Description

Function to estimate the time-varying mediation effect and bootstrap standard errors for three treatment groups and a continuous outcome.

#### Usage

```
tvma_3trt(
 T1,
 T2,
 t.seq,
 mediator,
 outcome,
 t.est = t.seq,
 plot = FALSE,
 CI = "boot",
 replicates = 1000,
 grpname = "T",
 verbose = FALSE
)
```

T1	a vector indicating assignment to treatment 1
Т2	a vector indicating assignment to treatment 2
t.seq	a vector of time points for each observation
mediator	matrix of mediator values in wide format
outcome	matrix of outcome values in wide format
t.est	a vector of time points at which to make the estimation. Default = t.seq. (OP-TIONAL ARGUMENT)
plot	TRUE or FALSE for plotting mediation effect. Default = "FALSE". (OP-TIONAL ARGUMENT)
CI	"none" or "boot" method of deriving confidence intervals. Default = "boot". (OPTIONAL ARGUMENT)
replicates	number of replicates for bootstrapping confidence intervals. Default = 1000. (OPTIONAL ARGUMENT)

verbose Default = "T". (OPTIONAL ARGUMENT) TRUE or FALSE for printing results to screen. Default = "FALSE". (OP TIONAL ARGUMENT)	grpname	name of the treatment arms (exposure groups) to be displayed in the results.
1 6		Default = "T". (OPTIONAL ARGUMENT)
	verbose	TRUE or FALSE for printing results to screen. Default = "FALSE". (OP-TIONAL ARGUMENT)

hat.alpha1 CI.lower.alpha1	estimated Treatment 1 effect on mediator
CI.upper.alpha1	CI lower limit for estimated coefficient hat.alpha1
	CI upper limit for estimated coefficient hat.alpha1
hat.alpha2 CI.lower.alpha2	estimated Treatment 2 effect on mediator
·	CI lower limit for estimated coefficient hat.alpha2
CI.upper.alpha2	2
	CI upper limit for estimated coefficient hat.alpha2
hat.gamma1 CI.lower.gamma1	estimated Treatment 1 direct effect on outcome
	CI lower limit for estimated coefficient hat.gamma1
CI.upper.gamma1	
	CI upper limit for estimated coefficient hat.gamma1
hat.gamma2 CI.lower.gamma2	
	CI lower limit for estimated coefficient hat.gamma2
CI.upper.gamma2	CI upper limit for estimated coefficient hat.gamma2
hat.tau1	estimated Treatment 1 total effect on outcome
CI.lower.tau1	CI lower limit for estimated coefficient hat.tau1
CI.upper.tau1	CI upper limit for estimated coefficient hat.tau1
hat.tau2	estimated Treatment 2 total effect on outcome
CI.lower.tau2	CI lower limit for estimated coefficient hat.tau2
CI.upper.tau2	CI upper limit for estimated coefficient hat.tau2
hat.beta	estimated mediator effect on outcome
CI.lower.beta	CI lower limit for estimated coefficient hat.beta
CI.upper.beta	CI upper limit for estimated coefficient hat.beta
hat.mediation1	time varying mediation effect for Treatment 1 on outcome
SE_MedEff1	estimated standard errors of hat.mediation1
CI.upper.T1	CI upper limit for hat.mediation1
CI.lower.T1	CI lower limit for hat.mediation1
hat.mediation2	time varying mediation effect for Treatment 2 on outcome
SE_MedEff2	estimated standard errors of hat.mediation2
CI.upper.T2	CI upper limit for hat.mediation2
CI.lower.T2	CI lower limit for hat.mediation2

#### tvma\_3trt

#### **Plot Returns**

- 1. plot1\_a1 plot for hat.alpha1 with CIs over t.est
- 2. plot2\_a2 plot for hat.alpha2 with CIs over t.est
- 3. plot3\_g1 plot for hat.gamma1 with CIs over t.est
- 4. plot4\_g2 plot for hat.gamma2 with CIs over t.est
- 5. plot5\_t1 plot for hat.tau1 with CIs over t.est
- 6. plot6\_t2 plot for hat.tau2 with CIs over t.est
- 7. plot7\_b plot for hat.beta with CIs over t.est
- 8. MedEff\_T1 plot for hat.mediation1 over t.est
- 9. MedEff\_T2 plot for hat.mediation2 over t.est
- 10. MedEff\_CI\_T1 plot for hat.mediation1 with CIs over t.est
- 11. MedEff\_CI\_T2 plot for hat.mediation2 with CIs over t.est

#### References

- 1. Fan, J. and Gijbels, I. Local polynomial modelling and its applications: Monographs on statistics and applied probability 66. CRC Press; 1996.
- Fan J, Zhang W. Statistical Estimation in Varying Coefficient Models. The Annals of Statistics. 1999;27(5):1491-1518.
- Fan J, Zhang JT. Two-step estimation of functional linear models with applications to longitudinal data. Journal of the Royal Statistical Society: Series B (Statistical Methodology). 2000;62(2):303-322.
- 4. Cai X, Coffman DL, Piper ME, Li R. Estimation and inference for the mediation effect in a time-varying mediation model. BMC Med Res Methodol. 2022;22(1):1-12.
- Baker TB, Piper ME, Stein JH, et al. Effects of Nicotine Patch vs Varenicline vs Combination Nicotine Replacement Therapy on Smoking Cessation at 26 Weeks: A Randomized Clinical Trial. JAMA. 2016;315(4):371.
- 6. B. Efron, R. Tibshirani. Bootstrap Methods for Standard Errors, Confidence Intervals, and Other Measures of Statistical Accuracy. Statistical Science. 1986;1(1):54-75.

#### Examples

# GENERATE TWO BINARY TREATMENT VARIABLES

tvmb

*Time Varying Mediation Function: Binary Outcome and Two Treatment Groups* 

#### Description

Function to estimate the time-varying mediation effect and bootstrap standard errors, involving two treatment groups and binary outcome.

#### Usage

```
tvmb(
   treatment,
   t.seq,
   mediator,
   outcome,
   span = 0.75,
   plot = FALSE,
   CI = "boot",
   replicates = 1000,
   verbose = FALSE
```

#### )

treatment	a vector indicating treatment group
t.seq	a vector of unique time points for each observation
mediator	matrix of mediator values in wide format
outcome	matrix of outcome values in wide format
span	Numeric value of the span to be used for LOESS regression. Default = $0.75$ .

#### tvmb

plot	TRUE or FALSE for producing plots. Default = "FALSE". (OPTIONAL AR-GUMENT)
CI	"none" or "boot" method of deriving confidence intervals. Default = "boot". (OPTIONAL ARGUMENT)
replicates	Number of replicates for bootstrapping confidence intervals. Default = 1000. (OPTIONAL ARGUMENT)
verbose	TRUE or FALSE for printing results to screen. Default = "FALSE". (OP-TIONAL ARGUMENT)

#### Value

timeseq	time points of estimation
alpha_hat	estimated treatment effect on mediator
CI.lower.a	CI lower limit for estimated coefficient alpha_hat
CI.upper.a	CI upper limit for estimated coefficient alpha_hat
gamma_hat	estimated treatment effect on outcome (direct effect)
CI.lower.g	CI lower limit for estimated coefficient gamma_hat
CI.upper.g	CI upper limit for estimated coefficient gamma_hat
beta_hat	estimated mediator effect on outcome
CI.lower.b	CI lower limit for estimated coefficient beta_hat
CI.upper.b	CI upper limit for estimated coefficient beta_hat
tau_hat	estimated treatment effect on outcome (total effect)
CI.lower.t	CI lower limit for estimated coefficient tau_hat
CI.upper.t	CI upper limit for estimated coefficient tau_hat
medEffect	time varying mediation effect
CI.lower	CI lower limit for medEffect
CI.upper	CI upper limit for medEffect

#### **Plot Returns**

- 1. plot1\_a plot for alpha\_hat with CIs over t.seq
- 2. plot2\_g plot for gamma\_hat with CIs over t.seq
- 3. plot3\_b plot for beta\_hat with CIs over t.seq
- 4. plot4\_t plot for tau\_hat with CIs over t.seq
- 5. MedEff plot for medEffect over t.seq
- 6. MedEff\_CI plot for medEffect with CIs over t.seq
- 7. bootstrap plot for estimated medEffect from bootstrapped samples over t.seq

#### Note

- 1. Currently supports 2 treatment groups
- 2. \*\* IMPORTANT \*\* An alternate way of formatting the data and calling the function is documented in detail in the tutorial for the tvmb() function.

#### References

- Fan, J. and Gijbels, I. Local polynomial modelling and its applications: Monographs on statistics and applied probability 66. CRC Press; 1996.
- 2. Fan J, Zhang W. Statistical Estimation in Varying Coefficient Models. The Annals of Statistics. 1999;27(5):1491-1518.
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#### Examples

```
## Not run: data(smoker)
# REDUCE DATA SET TO ONLY 2 TREATMENT CONDITIONS (EXCLUDE COMBINATION NRT)
smoker.sub <- smoker[smoker$treatment != 4, ]</pre>
# GENERATE WIDE FORMATTED MEDIATORS
mediator <- LongToWide(smoker.sub$SubjectID,</pre>
                        smoker.sub$timeseq,
                        smoker.sub$NegMoodLst15min)
# GENERATE WIDE FORMATTED OUTCOMES
outcome <- LongToWide(smoker.sub$SubjectID,</pre>
                       smoker.sub$timeseq,
                       smoker.sub$smoke_status)
# GENERATE A BINARY TREATMENT VARIABLE
trt <- as.numeric(unique(smoker.sub[, c("SubjectID","varenicline")])[, 2])-1</pre>
# GENERATE A VECTOR OF UNIQUE TIME POINTS
t.seq <- sort(unique(smoker.sub$timeseq))</pre>
# COMPUTE TIME VARYING MEDIATION ANALYSIS USING BOOTSTRAPPED CONFIDENCE INTERVALS
results <- tvmb(trt, t.seq, mediator, outcome)</pre>
## End(Not run)
```

tvmcurve\_3trt

Main function for time varying mediation function for continuous outcome and three treatment arms (i.e., exposure groups).

#### tvmcurve\_3trt

# Description

Part of the set of internal functions to estimate the time-varying mediation effect and bootstrap standard errors for three treatment groups and continuous outcome.

#### Usage

```
tvmcurve_3trt(T1, T2, t.seq, x, y, t.est)
```

# Arguments

T1	a vector indicating assignment to treatment 1
T2	a vector indicating assignment to treatment 2
t.seq	a vector of time points for each observation
x	matrix of mediator values in wide format
У	matrix of outcome values in wide format
t.est	time points at which to make the estimation. Default = t.seq

# Value

hat.alpha1	estimated Treatment 1 effect on mediator
hat.alpha2	estimated Treatment 2 effect on mediator
hat.gamma1	estimated Treatment 1 direct effect on outcome
hat.gamma2	estimated Treatment 2 direct effect on outcome
hat.tau1	estimated Treatment 1 total effect on outcome
hat.tau2	estimated Treatment 2 total effect on outcome
hat.beta	estimated mediator effect on outcome
hat.mediation1	time varying mediation effect for Treatment 1 on outcome
hat.mediation2	time varying mediation effect for Treatment 2 on outcome

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\* datasets smoker, 10 $bootci\_coeff\_2trt, 2$ bootci\_coeff\_3trt, 3 bootci\_coeff\_binary, 4 bootci\_tvm\_3trt, 6 bootci\_tvmb, 5 coeff, 7 estBootCIs, 8 estCoeff, 8 LongToWide, 9, 11  ${\tt newMediatorOutcome, 10}$ smoker, 10smoothest, 11tvma, *11*, 12 tvma\_3trt, *11*, 15 tvmb, *11*, 18

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